# **Examinable Topics for Revision**

ACTL3142 & ACTL5110 Statistical Machine Learning for Risk Applications



## Statistical Learning

- What is statistical (machine) learning? regression and classification problems
- prediction and inference
- interpretability and flexibility
- supervised and unsupervised learning

- mean squared error
- bias-variance trade-off
- K-nearest neighbors



# Linear Regression

- Linear Regression
- Simple Linear Regression
- Assumptions of the Model
- Least Squares Estimates (LSE)
- LSE Properties & Uncertainty
- Maximum Likelihood Estimates
- Confidence Intervals
- Multiple Linear Regression
- Qualitative predictors
- Linear Algebra / Matrix Approach

- Residual standard error (RSE)
- R-squared  $(R^2)$
- Linear model as an approximation
- Random error  $\epsilon$
- dummy variables
- Interaction terms  $(X_i X_j)$
- Quadratic terms  $(X_i^2)$



# Linear Regression II

- Linear Model Selection
  - Subset selection
  - Indirect methods
- Subset Selection
  - Best subset
  - Forward stepwise
  - Backwards stepwise
  - Hybrid stepwise
- $C_p$ , AIC, BIC, and Adjusted  $R^2$

- Problems with Linear Regression
  - Non-linearity of responsepredictor relationships
  - Correlation of error terms
  - Non-constant variance of error terms
  - Outliers, high-leverage points, collinearity, and confounding effects



# Logistic Regression

- binary classification
- Logistic regression
- odds, log-odds
- logits
- error rate (misclassification)

- confusion matrix
- thresholds
- ROC curve
- AUC
- Poisson regression



#### Generalised Linear Models

- generalised linear models
- link functions
- distributions
- exponential family
- mean function
- variance function

- canonical link functions
- null model
- full model
- deviance & scaled deviance
- residuals
- degrees of freedom



### Cross-validation and regularisation

- Train, validation & test sets
- Validation Set Approach
- *k*-fold Cross-Validation
- Leave-One-Out Cross-Validation
- Test error

- Regularisation (shrinkage)
  - ridge
  - lasso
  - elastic net



## Moving Beyond Linearity

- interpolation & extrapolation
- polynomial regression
  - monomials
  - orthogonal polynomials
- step functions
  - basis function expansion
  - piecewise polynomial functions

- regression splines
  - knots
  - natural splines
  - cubic splines
- smoothing splines
- local regression
- generalised additive models (GAMs)

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#### Tree-based Methods

- decision trees
- classification trees
- regression trees
- pruning
- ensemble methods

- bagging
- random forests
- boosting
- gradient boosting



# Unsupervised Learning

- *k*-means clustering
- hierarchical clustering
- principal components analysis

